

Strategic Hypothesis Testing

NeurIPS 2025 · Spotlight



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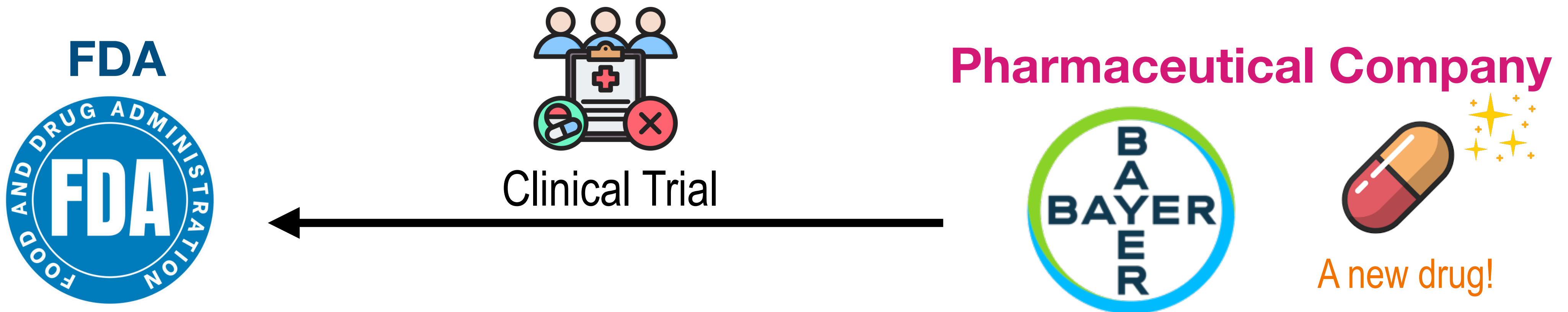
**equal contribution*

My Research

- My research lies in the intersections of **Game Theory, Machine Learning and Decision-Making**
 - how **strategic** human agents interact with ML systems?
 - how **incentives from the decision rule** shape the outcomes of algorithmic decisions
- This paper fits into this theme!

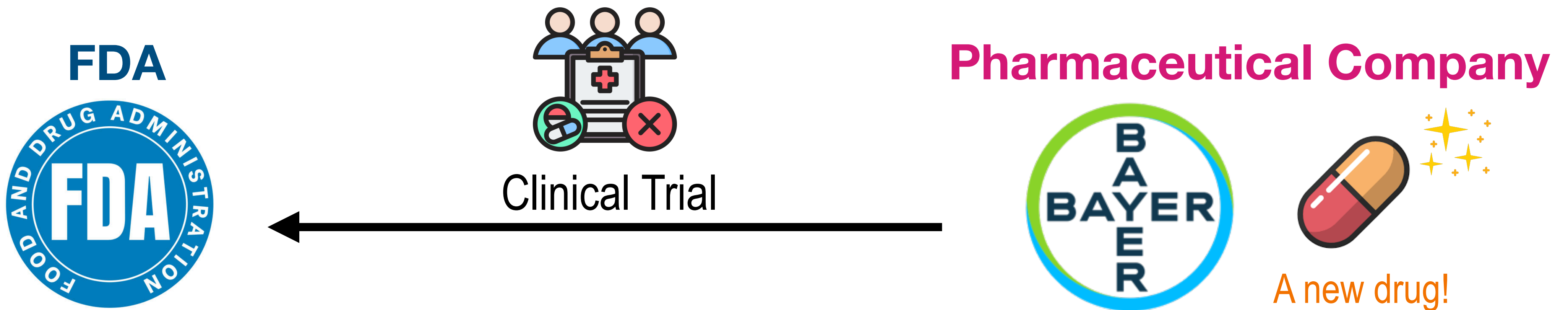
Decision-Making Based on Statistical Evidence

- Many real-life decisions have to rely on (noisy) evidence from a statistical test
- Example: the FDA's drug approval process

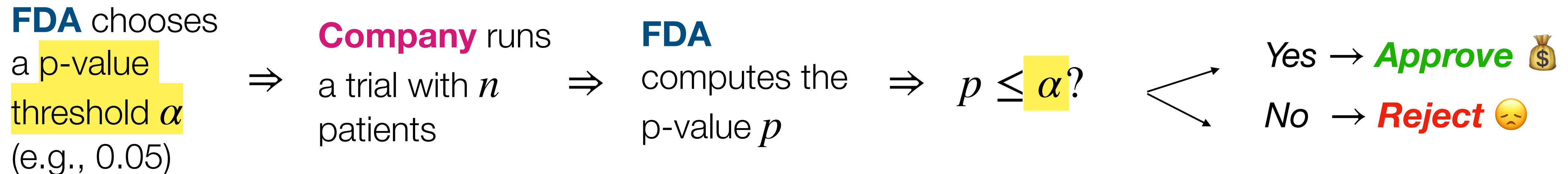


- **FDA's decision** (Approve ✓ or Reject ✗) on the drug is entirely based on clinical trial results

Decision-Making Based on Statistical Evidence



FDA's Testing Protocol



Drug Company's Decision & Utility

FDA's Testing Protocol

⇒ **Company** runs
a trial with n
patients

⇒ $p \leq \alpha?$ 

- **Company** (with effectiveness μ) chooses the size of the clinical trial n^* to maximize the expected utility

For any fixed rule α , sample size $n \uparrow$
⇒ $Pr[\text{approve} | n, \alpha] \uparrow$ but $Cost(n) \uparrow$

$$u(n; \alpha) = R \cdot \Pr[\text{approve} | n, \alpha] - \text{Cost}(n)$$

Revenue once
approved   

Cost of the trial
(with n samples)


Company will do strategic self-selection:
If $u(n^*; \alpha) < 0$, agent will not participate

FDA's Decision & Utility

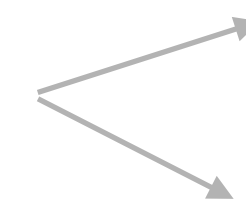
FDA's Testing Protocol

FDA chooses
a p-value
threshold α
(e.g., 0.05)

\Rightarrow

\Rightarrow

$\Rightarrow p \leq \alpha?$



- **The FDA**, knowing **agents** will do a **strategic self-selection**, chooses α^* to minimize total errors

$$u(n; \alpha) = R \cdot \Pr[\text{approve} \mid n, \alpha] - \text{Cost}(n)$$



$$\ell(\alpha) = \mathbb{E}_Q[\lambda_1 \text{FP} + \lambda_2 \text{FN}]$$

Approve inefficient
drug

Disapprove effective drug/
effective drug not
participate

Results & Implications

- We provide characterizations of the **optimal behavior** of both **the principal** (selection criteria α^*) and **the agent** (optimal size of the trial n^*)
 - We characterize how different loss components (FP, FN) change as we vary α
 - They are still monotonic in α (same as in classic hypothesis testing!)
- Our results offer insights for **policymakers/regulators**
 - **Agent's** strategic self-selection works **in favor of the principal!**

Proposition $\forall \alpha > 0$, there exists a participation threshold $\mu_\tau(\alpha)$, s.t. only drug with effectiveness $\mu \geq \mu_\tau(\alpha)$ will participate. $\mu_\tau(\alpha)$ is monotonic in α .

- **Principal** can choose a stricter α so only good **agents** participate

Final Remarks

- A statistical decision-rule on strategic agents **not only makes decisions** — it also acts as a **gatekeeper**, shaping who chooses to participate.
- Our model can be used to study much broader settings:
 - A/B testing for a new feature
 - Scientific discovery
 - Etc...

Thank you! Question?